# The Stereochemical Effect of $6 \mathbf{s}^{\mathbf{2}}$ Lone-Pair Electrons: The Crystal Structure of a New Lead Bismuth Oxyphosphate $\mathrm{Pb}_{4} \mathrm{BiO}_{4} \mathrm{PO}_{4}$ 

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$\mathrm{Pb}_{4} \mathrm{BiO}_{4} \mathrm{PO}_{4}$ was prepared by heating a stoichiometric mixture of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}, \mathrm{PbO}$, and $\mathrm{Bi}_{2} \mathrm{O}_{3}$ at $700^{\circ} \mathrm{C}$ for 4 days with intermediate grinding. The material melts congruently at $805^{\circ} \mathrm{C}$; single crystals were obtained by slow cooling of a melt. The compound is triclinic, $P \overline{1}, a=6.215(1) \AA, b=7.440(2) \AA, c=$ $10.498(2) \AA, \alpha=100.19(1)^{\circ}, \beta=103.73(1)^{\circ}, \gamma=90.05(1)^{\circ}, Z=2$. The structure refinement converged to $R=0.0485$. Bi is bonded to 4 O at distances varying from $2.16(3) \AA$ to $2.53(3) \AA$ and two bonds at $3.10(3) \AA$ and $3.15(3) \AA$. Five atoms form an almost perfect pentagon parallel to (001) with an apical $\mathrm{Bi}-\mathrm{O}$ bond nearly perpendicular to the pentagonal plane. Presumably the lone pair points to the empty apex to complete a pentagonal bipyramid. $\mathrm{Pb}(1)$ is bonded to seven oxygen atoms. Five of these bonds are less than $2.9 \AA$, while two are $3.12(3) \AA$ and $3.16(3) \AA$. Four oxygen atoms constitute the equatorial plane of an octahedron with $\mathrm{Pb}(1)$ slightly out of that plane. The apex oxygen atoms are tilted in the same direction away from the normal to the equatorial plane. One triangular face is capped by an oxygen atom while another triangular face is open and the lone pair electrons cap this face. $\mathrm{Pb}(2), \mathrm{Pb}(3)$, and $\mathrm{Pb}(4)$ have similar coordination polyhedra. The average of the four $\mathrm{P}-\mathrm{O}$ bonds is $1.53(5) \AA$. The $\mathrm{Pb}-\mathrm{O}$ framework is related to that of tetragonal PbO and the structure is related to that of $\mathrm{Pb}_{5} \mathrm{SO}_{8}$. The valence bond sums for two of the $\mathbf{P b}$ atoms are 2.63 and 2.32 , while the other two Pb atoms have the more expected values, 2.14 and 2.06. The valence bond sum for Bi is 2.14 , much less than the expected trivalent oxidation state. Van der Waals contacts exist between the two Pb with the increased oxidation states and Bi but no contacts exist between the other two Pb and Bi . Where van der Waals contacts are present the $\mathbf{P b} 6 \mathbf{s}^{2}$ energy levels overlap the empty Bi 6p energy levels so that electron transfer into the Bi 6p levels from $\mathbf{P b}$ occurs. The electrons are not itinerant because of the large atomic separations and the material remains insulating. (C) 1999 Academic Press

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## INTRODUCTION

The discovery that $\mathrm{Bi}_{4} \mathrm{~V}_{2} \mathrm{O}_{11}$ is a good oxide ion conductor has led to intense research on this compound. Numerous attempts have been reported to improve the ion conductivity by isovalent and aliovalent substitution of the transition metal and of bismuth. The $\mathrm{Bi}-\mathrm{P}(\mathrm{V})-\mathrm{O}$ system (1-4) and the pseudoternary systems $\mathrm{Bi}_{2} \mathrm{O}_{3}-\mathrm{PbO}-M_{2} \mathrm{O}_{5}$, where $M=$ $\mathrm{P}, \mathrm{V}, \mathrm{As}$, have been extensively investigated (5-7) in the expectation that some of the compounds will display interesting physical properties such as improved anionic conduction. Mizrahi et al. (5) described new phases with $M=\mathrm{V}$ and, in particular, $\mathrm{Pb}_{4} \mathrm{BiVO}_{8}$. Unfortunately the crystals were of poor quality and no structure for this compound was determined. Surprisingly, numerous compounds with related stoichiometries, $\mathrm{Pb}_{5} \mathrm{SO}_{8}(8,9), \mathrm{Pb}_{5} \mathrm{CrO}_{8}(10,11)$, $\mathrm{Pb}_{5} \mathrm{SeO}_{8}$ (11), $\mathrm{Pb}_{5}\left(\mathrm{Cr}_{1-x} \mathrm{~S}_{x}\right) \mathrm{O}_{8}$ (12), and $\mathrm{Pb}_{5} \mathrm{MoO}_{8}$ (13), were only partially characterized due to commensurate and incommensurate modulations present in their structures. Precise oxygen atomic positions were not even available for $\mathrm{Pb}_{5} \mathrm{SO}_{8}$, which was widely studied because of applications in lead-acid battery technology. Only recently has its crystal structure been solved (14) and shown to be closely related to the structure of PbO . We report here the structure of a new compound, $\mathrm{Pb}_{4} \mathrm{BiO}_{4} \mathrm{PO}_{4}$ (hereafter $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ ), with a similar stoichiometry.

## EXPERIMENTAL

Polycrystalline samples were prepared by solid state reaction of stoichiometric proportions of $\left(\mathrm{NH}_{4}\right)_{2} \mathrm{HPO}_{4}, \mathrm{PbO}$, and $\mathrm{Bi}_{2} \mathrm{O}_{3}$. Prior to use the oxides were preheated overnight at $600^{\circ} \mathrm{C}$ to remove any carbonate. After thorough grinding, the powder was slowly heated at $300^{\circ} \mathrm{C}$ until the diammonium hydrogen phosphate had completely decomposed. The reaction was completed after annealing at $700^{\circ} \mathrm{C}$ for 4 days with intermediate grinding. The samples were examined by X-ray diffraction with a Guinier-de Wolff
camera and $\mathrm{Cu} \mathrm{K} \alpha$ radiation. A final pattern was recorded on an automated D5000 Siemens diffractometer and completely indexed using TREOR (15). Density measurements were performed with an automated Micromeritics Accupyc 1330 gas pycnometer equipped with a $1 \mathrm{~cm}^{3}$ cell. Differential thermal analysis (DTA) was done on a Du Pont 1090B thermal analyzer using a 1600 differential thermal analysis cell with a heating rate of $5^{\circ} \mathrm{C} \mathrm{min}^{-1}$. The possibility of phase transitions was checked with a high temperature X-ray diffraction (HTXRD) Guinier-Lenné camera at a heating rate of $20^{\circ} \mathrm{C} \mathrm{min}^{-1}$.

Single crystals of $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ were obtained by melting of polycrystalline samples and slow cooling in a gold crucible. $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ melts congruently at $805^{\circ} \mathrm{C}$ without an intermediate phase transition. The temperature was raised to $840^{\circ} \mathrm{C}$ at $250^{\circ} \mathrm{C} / \mathrm{h}$, held at $840^{\circ} \mathrm{C}$ for 3 h , cooled to $725^{\circ} \mathrm{C}$ at $1^{\circ} \mathrm{C} / \mathrm{h}$ and then furnace cooled to room temperature. The crystals are light yellow needles. Weissenberg photographs were used to determine the quality of the crystals. The data for the structure determination were recorded on a Siemens P 4 diffractometer. The pertinent data are summarized in Table 1. An absorption correction using SHELXTL-PLUS (16) was applied. SHELXS-86 (17) was used to find the structure solution and the refinement was performed with SHELXL93 (18). The structure was solved using the Patterson method and refined by full-matrix least squares. The $\mathrm{Pb}, \mathrm{Bi}$, and P atoms were refined anisotropically, while O atoms were refined isotropically. The least-squares refinement was based on 1494 observed reflections, $I>2 \sigma(I)$, and 88 variable parameters and converged to $R=0.0485$.

## RESULTS

All observed lines of the powder pattern were indexed using TREOR. Lattice constants indicated the isostructural nature of $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ and $\mathrm{Pb}_{4} \mathrm{BiVO}_{8}$ (5). The parameters were refined by least squares to $a=6.229(2) \AA, b=$ 7.433(3) $\AA, c=10.494(2) \AA, \alpha=100.12(2)^{\circ}, \beta=103.88(2)^{\circ}$, $\gamma=90.14(2)^{\circ}$ and differ slightly from those obtained from the single crystal (Table 1). The figures of merit were $F(30)=29.3(0.015,0.68)$ and $M(20)=20.9(3.1015,32)(15)$. Table 2 lists the indexed powder X-ray diffraction pattern. The measured density, $\rho=8.636 \mathrm{~g} / \mathrm{cm}^{3}$, yields two formula weights per unit cell. DTA and HTXRD investigations did not show any phase transition occuring between room temperature and the melting temperature at $805^{\circ} \mathrm{C}$.

Initially neither a Patterson map nor direct methods yielded a valid structural model. A trial model was constructed in the acentric space group P 1 . Two Pb atoms were first introduced in 000 and $01 / 20$ positions and the remaining 6 Pb and 2 Bi atoms were successively introduced and refined in positions identified from the Patterson map. At this stage the refinement converged to $R=0.14$. A

TABLE 1 Crystal Data and Intensity Collection

| Crystallographic data |  |
| :---: | :---: |
| Formula | $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ |
| Color | Light yellow |
| Crystal system | Triclinic |
| Space group | $\mathrm{P} \overline{1}$ |
| $a(\AA)$ | 6.215(1) |
| $b(\AA)$ | 7.440(2) |
| $c(\AA)$ | 10.498(2) |
| $\alpha$ | $100.19(1)^{\circ}$ |
| $\beta$ | 103.73(1) ${ }^{\circ}$ |
| $\gamma$ | $90.05(1)^{\circ}$ |
| Volume ( $\AA^{3}$ ) | 463.6 |
| $Z$ | 2 |
| Formula weight (g/mol) | 1196.71 |
| Measured density (g/cm ${ }^{3}$ ) | 8.64 |
| Calculated density ( $\mathrm{g} / \mathrm{cm}^{3}$ ) | 8.58 |
| Intensity collection |  |
| Diffractometer | Siemens P4 |
| Radiation ( $\AA$ ) | MoK $\alpha, \lambda=0.7107$ |
| Monochromator | Graphite |
| Temperature ( ${ }^{\circ} \mathrm{C}$ ) | 23 |
| Scan method | $\omega, 1^{\circ}$ |
| $\theta$ Range | 2.03-27.48 ${ }^{\circ}$ |
| Data collected | $\begin{aligned} & -8 \leq h \leq 7, \quad-9 \leq k \leq 9, \\ & 0 \leq l \leq 13 \end{aligned}$ |
| No of reflections measured/independent | 2712/2126 |
| No of unique reflections $I>2 \sigma(I)$ | 1494 |
| $\mu\left(\mathrm{cm}^{-1}\right)$ | 915 |
| $R_{\text {int }}$ | 0.0438 |
| Absorption correction | SHELXTL-PLUS |
| Transmission factor | 0.02612-0.08674 |
| Indices of single crystal faces $h, k, l /$ dimensions (mm) $\overline{1} 00 / 0.02 ; 100 / 0.02$; $010 / 0.12 ; 0 \overline{1} 0 / 0.12 ; 001 / 0.02 ; 00 \overline{1} / 0.02$ <br> Refinement |  |
| Parameters varied | 88 |
| Refinement method | Least squares on $F^{2}$ |
| $R(F)$ | 0.0485(obs)/0.0823(all) |
| $R_{\text {w }}\left(F^{2}\right)$ | 0.1011 (obs)/0.1159(all) |
| $w=1 /\left(\sigma^{2}\left(\mathrm{Fo}^{2}\right)+(0.0493 P)^{2}+9.2976 P\right)$ with $P=\left(\mathrm{Fo}^{2}+2 \mathrm{Fc}^{2}\right) / 3$ |  |
| Extinction correction | $0.0018 \times 10^{-3}$ |
| GOF | $1.098(\mathrm{obs}) / 1.028(\mathrm{all})$ |
| Max., min., $\Delta \rho$, e $\AA^{-3}$ | 2.88, - 3.09 |

centrosymmetric origin was then identified and the appropriate translation applied to the atomic parameters. A refinement in space group $\mathrm{P} \overline{1}$, with isotropic displacement parameters yielded a conventional $R=0.08$. The oxygen atomic positions were now obtained from successive Fourier electron density difference maps and introduced into the refinement process. The final least squares refinement with anisotropic displacement parameters for the heavy atoms and isotropic for oxygen yielded $R=0.0485$. Table 3 lists the final atomic parameters, Table 4 the anisotropic displacement parameters, and significant interatomic bond lengths and angles are shown in Table 5.

TABLE 2
The Powder X-Ray Diffraction Diagram of $\mathrm{Pb}_{\mathbf{4}} \mathrm{BiO}_{4} \mathrm{PO}_{4}$

| $h$ | $k$ | $l$ | $d$ obs. $\AA$ | $d$ calc. $\AA$ | I/Io (\%) |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 1 | 10.010 | 10.018 | 2 |
| 0 | 1 | $-1$ | 6.494 | 6.493 | $<1$ |
| 1 | 0 | 0 | 6.047 | 6.040 | <1 |
| 1 | 0 | $-1$ | 5.844 | 5.842 | 1 |
| 0 | 1 | 1 | 5.460 | 5.452 | 1 |
| 0 | 0 | 2 | 5.006 | 5.009 | 1 |
| 1 | $-1$ | 0 | 4.771 | 4.767 | $<1$ |
| 1 | 0 | 1 | 4.694 | 4.691 | 1 |
| 0 | 1 | -2 | 4.537 | 4.534 | 1 |
| 1 | 0 | -2 | 4.425 | 4.423 | $<1$ |
| 1 | $-1$ | 1 | 4.179 | 4.185 | <1 |
| 1 | 1 | -2 | 4.015 | 4.015 | 1 |
| 0 | 1 | 2 | 3.821 | 3.821 | 1 |
| 1 | 1 | 1 | 3.748 | 3.747 | $<1$ |
| 0 | 2 | -1 | 3.650 | 3.654 | 1 |
| 1 | 0 | 2 | 3.460 | 3.463 | 2 |
| 0 | 0 | 3 | 3.339 | 3.339 | 100 |
| 1 | 0 | $-3$ | 3.280 | 3.281 | 11 |
| 0 | 2 | -2 | 3.248 | 3.246 | 5 |
| 2 | 0 | -1 | 3.112 | 3.109 | 1 |
| 1 | 2 | 0 | 3.060 | 3.064 | 1 |
| 2 | 0 | 0 | 3.021 | 3.020 | 13 |
| 1 | -2 | -1 | 3.016 | 3.017 | 26 |
| 2 | -1 | -1 | 2.854 | 2.852 | 1 |
| 2 | -1 | 0 | 2.842 | 2.838 | $<1$ |
| 1 | -2 | 2 | 2.731 | 2.730 | 19 |
| 1 | 0 | 3 | 2.661 | 2.660 | 9 |
| 2 | 0 | -3 | 2.573 | 2.574 | 4 |
| 0 | 0 | 4 | 2.504 | 2.505 | 8 |
| 2 | -2 | 0 | 2.384 | 2.383 | 1 |
| 2 | 2 | -2 | 2.354 | 2.353 | 1 |
| 1 | -3 | 0 | 2.297 | 2.297 | 3 |
| 2 | -2 | 1 | 2.280 | 2.281 | 2 |
| 0 | 2 | -4 | 2.268 | 2.267 | 3 |
| 1 | 3 | 0 | 2.225 | 2.224 | 1 |
| 2 | 1 | 2 | 2.156 | 2.158 | $<1$ |
| 1 | 0 | 4 | 2.138 | 2.136 | 1 |
| 2 | -2 | 2 | 2.093 | 2.093 | 2 |
| 3 | 0 | -1 | 2.074 | 2.074 | 1 |
| 1 | 0 | -5 | 2.057 | 2.058 | 1 |
| 2 | -1 | 3 | 2.010 | 2.011 | 2 |
| 1 | -2 | -4 | 1.943 | 1.943 | 2 |
| 2 | 3 | $-1$ | 1.926 | 1.926 | 1 |
| 0 | 2 | 4 | 1.910 | 1.911 | 8 |
| 0 | 4 | -1 | 1.860 | 1.858 | 4 |
| 3 | 2 | -2 | 1.810 | 1.808 | 4 |
| 2 | 2 | -5 | 1.792 | 1.791 | 3 |
| 1 | 4 | -1 | 1.775 | 1.775 | 1 |
| 1 | -3 | 4 | 1.763 | 1.763 | $<1$ |
| 3 | 2 | 0 | 1.730 | 1.730 | 2 |
| 1 | -2 | 5 | 1.720 | 1.720 | 7 |
| 1 | 2 | -6 | 1.672 | 1.673 | 2 |
| 1 | 1 | 5 | 1.662 | 1.661 | 1 |
| 3 | 2 | 1 | 1.626 | 1.626 | 4 |
| 2 | -4 | 1 | 1.584 | 1.584 | 2 |
| 2 | 4 | - 3 | 1.565 | 1.566 | 1 |
| 4 | $-1$ | -1 | 1.522 | 1.522 | 3 |
| 1 | 0 | 6 | 1.517 | 1.517 | 1 |
| 4 | 0 | 0 | 1.510 | 1.510 | 2 |
| 3 | - 3 | -3 | 1.478 | 1.478 | 1 |

Note. The lattice parameters are $a=6.229(2) \AA, b=7.443(3) \AA, c=$ 10.494(2) $\AA, \alpha=100.12(2)^{\circ}, \beta=103.88(2)^{\circ}, \gamma=90.14(2)^{\circ}, \mathrm{CuK} \alpha$.

TABLE 3 Atomic Coordinates and Equivalent Displacement Parameters, $\AA^{2}$, for $\mathrm{Pb}_{4} \mathrm{BiO}_{4} \mathbf{P O}_{4}$

| Atom | $x$ | $y$ | $z$ | $U_{\text {eq }}$ |
| :--- | :---: | :---: | :---: | :---: |
| $\mathrm{Pb}(1)$ | $0.2386(2)$ | $0.0351(2)$ | $0.70334(9)$ | $0.0181(2)$ |
| $\mathrm{Pb}(2)$ | $0.2321(2)$ | $0.5641(2)$ | $0.70344(9)$ | $0.0187(2)$ |
| $\mathrm{Pb}(3)$ | $0.7330(2)$ | $-0.3815(2)$ | $0.96585(9)$ | $0.0163(2)$ |
| $\mathrm{Pb}(4)$ | $0.7347(2)$ | $0.1154(2)$ | $0.9644(1)$ | $0.0199(3)$ |
| Bi | $0.3070(2)$ | $0.2268(2)$ | $0.4099(1)$ | $0.0164(2)$ |
| P | $0.768(2)$ | $0.2945(9)$ | $0.6821(7)$ | $0.018(2)$ |
| $\mathrm{O}(1)$ | $0.650(3)$ | $-0.604(2)$ | $0.078(2)$ | $0.011(3)$ |
| $\mathrm{O}(2)$ | $0.645(3)$ | $-0.106(3)$ | $0.085(2)$ | $0.016(3)$ |
| $\mathrm{O}(3)$ | $0.034(3)$ | $-0.185(3)$ | $0.743(2)$ | $0.017(4)$ |
| $\mathrm{O}(4)$ | $0.001(4)$ | $0.306(3)$ | $0.777(2)$ | $0.029(4)$ |
| $\mathrm{O}(5)$ | $0.484(4)$ | $0.188(3)$ | $0.254(3)$ | $0.035(5)$ |
| $\mathrm{O}(6)$ | $0.263(4)$ | $0.563(4)$ | $0.400(3)$ | $0.046(6)$ |
| $\mathrm{O}(7)$ | $0.735(4)$ | $0.111(4)$ | $0.590(3)$ | $0.041(5)$ |
| $\mathrm{O}(8)$ | $0.588(4)$ | $0.308(3)$ | $0.768(2)$ | $0.035(5)$ |

## DISCUSSION

The presence of the lone-pair electrons on $\mathrm{Bi}^{3+}$ and $\mathrm{Pb}^{2+}$ distorts the oxygen coordination polyhedra by leaving a vacancy at a corner or lengthens a bond to an anion to a van der Waals contact, usually resulting in a lowering of the crystal system and/or space group. Both of these effects are seen in this structure.

Bi is bonded to 4 O at distances varying from $2.16(3) \AA$ to 2.53(3) $\AA$ and two bonds at $3.10(3) \AA$ and $3.15(3) \AA$ (Table 5). The five atoms, $\mathrm{O}(6), \mathrm{O}(6), \mathrm{O}(3), \mathrm{O}(7), \mathrm{O}(7)$, form an almost perfect pentagon parallel to (001) with $\mathrm{Bi}-\mathrm{O}(5)$ nearly perpendicular to the pentagonal plane (Fig. 1a). Presumably the lone-pair points to the empty apex to complete a pentagonal bipyramid. If the two long $\mathrm{Bi}-\mathrm{O}$ bonds are omitted from the coordination polyhedron then $\mathrm{O}(5)-\mathrm{O}(3)-\mathrm{O}(7)-$ $\mathrm{O}(6)$ form a trigonal bipyramid with the lone-pair occupying one apex.
$\mathrm{Pb}(1)$ is bonded to seven oxygen atoms. Five of these bonds are less than $2.9 \AA$, while two are $3.12(3) \AA$ and $3.16(3) \AA$. Four oxygen atoms, $O(3), O(4), O(8), O(5)$,

TABLE 4
Anisotropic Displacement Parameters

| Atom | $U_{11}$ | $U_{22}$ | $U_{33}$ | $U_{23}$ | $U_{13}$ | $U_{12}$ |
| :--- | :--- | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~Pb}(1)$ | $0.0204(5)$ | $0.0176(5)$ | $0.0162(4)$ | $0.0015(4)$ | $0.0056(4)$ | $-0.0015(4)$ |
| $\mathrm{Pb}(2)$ | $0.0203(5)$ | $0.0199(5)$ | $0.0164(5)$ | $0.0045(4)$ | $0.0047(4)$ | $0.0046(4)$ |
| $\mathrm{Pb}(3)$ | $0.0142(5)$ | $0.0133(5)$ | $0.0229(5)$ | $0.0027(4)$ | $0.0082(4)$ | $0.0007(4)$ |
| $\mathrm{Pb}(4)$ | $0.0147(5)$ | $0.0176(5)$ | $0.0324(6)$ | $0.0107(4)$ | $0.0109(4)$ | $0.0046(4)$ |
| Bi | $0.0163(5)$ | $0.0168(5)$ | $0.0163(4)$ | $0.0037(3)$ | $0.0037(3)$ | $0.0018(4)$ |
| P | $0.019(3)$ | $0.013(3)$ | $0.022(3)$ | $0.004(3)$ | $0.006(3)$ | $-0.001(3)$ |

TABLE 5
Bond lengths $(\AA)$, Angles $\left({ }^{\circ}\right)$, and Bond Valences for $\mathbf{P b}_{4} \mathbf{B i P O}_{8}{ }^{\boldsymbol{a}}$

|  | Bond lengths | Bond valences |  | Angles |  | Bond lengths | Bond valences |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{Bi}-\mathrm{O}(3)$ | 2.32(2) | 0.54 | $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(5)$ | 92(1) | $\mathrm{Pb}(1)-\mathrm{O}(2)$ | 2.14(2) | 0.93 |
| $\mathrm{Bi}-\mathrm{O}(5)$ | 2.16 (3) | 0.84 | $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(6)$ | 85(1) | $\mathrm{Pb}(1)-\mathrm{O}(3)$ | 2.23(2) | 0.73 |
| $\mathrm{Bi}-\mathrm{O}(6)$ | 2.53(3) | 0.31 | $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(6)$ | 158(1) | $\mathrm{Pb}(1)-\mathrm{O}(4)$ | 2.62(2) | 0.25 |
| $\mathrm{Bi}-\mathrm{O}(6)$ | 3.15(3) | 0.06 | $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(7)$ | 156(1) | $\mathrm{Pb}(1)-\mathrm{O}(5)$ | 2.41(3) | 0.45 |
| $\mathrm{Bi}-\mathrm{O}(7)$ | 2.52(3) | 0.32 | $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(7)$ | 85(1) | $\mathrm{Pb}(1)-\mathrm{O}(7)$ | 3.16 (3) | 0.06 |
| $\mathrm{Bi}-\mathrm{O}(7)$ | 3.10(3) | 0.07 | $\mathrm{O}(5)-\mathrm{Bi}-\mathrm{O}(6)$ | 92(1) | $\mathrm{Pb}(1)-\mathrm{O}(7)$ | 3.12(3) | 0.07 |
|  |  | 2.14 | $\mathrm{O}(5)-\mathrm{Bi}-\mathrm{O}(6)$ | 88(1) | $\mathrm{Pb}(1)-\mathrm{O}(8)$ | 2.85(3) | 0.14 |
|  |  |  | $\mathrm{O}(5)-\mathrm{Bi}-\mathrm{O}(7)$ | 86(1) |  |  | 2.63 |
|  |  |  | $\mathrm{O}(5)-\mathrm{Bi}-\mathrm{O}(7)$ | 94(1) |  |  |  |
|  |  |  | $\mathrm{O}(6)-\mathrm{Bi}-\mathrm{O}(6)$ | 73(1) | $\mathrm{Pb}(2)-\mathrm{O}(1)$ | 2.20(2) | 0.79 |
|  |  |  | $\mathrm{O}(6)-\mathrm{Bi}-\mathrm{O}(7)$ | 119(1) | $\mathrm{Pb}(2)-\mathrm{O}(3)$ | 2.27(2) | 0.65 |
|  |  |  | $\mathrm{O}(6)-\mathrm{Bi}-\mathrm{O}(7)$ | 168(1) | $\mathrm{Pb}(2)-\mathrm{O}(4)$ | 2.72(3) | 0.19 |
|  |  |  | $\mathrm{O}(6)-\mathrm{Bi}-\mathrm{O}(7)$ | 45(1) | $\mathrm{Pb}(2)-\mathrm{O}(5)$ | 2.46(3) | 0.39 |
|  |  |  | $\mathrm{O}(6)-\mathrm{Bi}-\mathrm{O}(7)$ | 117(1) | $\mathrm{Pb}(2)-\mathrm{O}(6)$ | 3.24(3) | 0.05 |
|  |  |  | $\mathrm{O}(7)-\mathrm{Bi}-\mathrm{O}(7)$ | 72(1) | $\mathrm{Pb}(2)-\mathrm{O}(6)$ | 3.10(3) | 0.07 |
|  |  |  |  |  | $\mathrm{Pb}(2)-\mathrm{O}(8)$ | 2.96 (3) | 0.10 |
|  |  |  |  |  |  |  | 2.26 |
| $\mathrm{P}-\mathrm{O}(4)$ | 1.54(2) | 1.23 | $\mathrm{O}(4)-\mathrm{P}-\mathrm{O}(6)$ | 113(2) |  |  |  |
| $\mathrm{P}-\mathrm{O}(6)$ | 1.47(3) | 1.49 | $\mathrm{O}(4)-\mathrm{P}-\mathrm{O}(7)$ | 109(2) | $\mathrm{Pb}(3)-\mathrm{O}(1)$ | 2.32(2) | 0.57 |
| $\mathrm{P}-\mathrm{O}(7)$ | 1.51(3) | 1.34 | $\mathrm{O}(4)-\mathrm{P}-\mathrm{O}(8)$ | 109(2) | $\mathrm{Pb}(3)-\mathrm{O}(1)$ | 2.31(2) | 0.59 |
| $\mathrm{P}-\mathrm{O}(8)$ | 1.59(3) | 1.08 | $\mathrm{O}(6)-\mathrm{P}-\mathrm{O}(7)$ | 108(2) | $\mathrm{Pb}(3)-\mathrm{O}(2)$ | 2.34(2) | 0.54 |
|  |  | 5.14 | $\mathrm{O}(6)-\mathrm{P}-\mathrm{O}(8)$ | 110(2) | $\mathrm{Pb}(3)-\mathrm{O}(4)$ | 3.47(2) | 0.03 |
|  |  |  | $\mathrm{O}(7)-\mathrm{P}-\mathrm{O}(8)$ | 108(2) | $\mathrm{Pb}(3)-\mathrm{O}(4)$ | 2.77(2) | 0.17 |
|  |  |  |  |  | $\mathrm{Pb}(3)-\mathrm{O}(5)$ | 2.99(3) | 0.09 |
| $\mathrm{Bi}-\mathrm{Pb}(1)$ | 3.73(1) |  | $\mathrm{Pb}(2)-\mathrm{O}(1)-\mathrm{Pb}(3)$ | 119.6(5) | $\mathrm{Pb}(3)-\mathrm{O}(8)$ | 2.81(2) | 0.15 |
| $\mathrm{Bi}-\mathrm{Pb}(1)$ | 3.74(1) |  | $\mathrm{Pb}(2)-\mathrm{O}(1)-\mathrm{Pb}(3)$ | 105.9(5) |  |  | 2.14 |
| $\mathrm{Bi}-\mathrm{Pb}(1)$ | 3.74(1) |  | $\mathrm{Pb}(2)-\mathrm{O}(1)-\mathrm{Pb}(4)$ | 114.5(5) |  |  |  |
| $\mathrm{Bi}-\mathrm{Pb}(2)$ | 3.74(1) |  | $\mathrm{Pb}(3)-\mathrm{O}(1)-\mathrm{Pb}(3)$ | 104.7(5) | $\mathrm{Pb}(4)-\mathrm{O}(1)$ | 2.34(2) | 0.54 |
| $\mathrm{Bi}-\mathrm{Pb}(2)$ | 3.72(1) |  | $\mathrm{Pb}(3)-\mathrm{O}(1)-\mathrm{Pb}(4)$ | 106.7(4) | $\mathrm{Pb}(4)-\mathrm{O}(2)$ | 2.39(2) | 0.47 |
| $\mathrm{Bi}-\mathrm{Pb}(2)$ | 3.78(1) |  | $\mathrm{Pb}(3)-\mathrm{O}(1)-\mathrm{Pb}(4)$ | 103.8(4) | $\mathrm{Pb}(4)-\mathrm{O}(2)$ | 2.29(2) | 0.62 |
|  |  |  |  |  | $\mathrm{Pb}(4)-\mathrm{O}(3)$ | 3.02(2) | 0.09 |
| $\mathrm{Bi}-\mathrm{P}$ | 3.50(1) |  | $\mathrm{Pb}(1)-\mathrm{O}(2)-\mathrm{Pb}(3)$ | 121.5(6) | $\mathrm{Pb}(4)-\mathrm{O}(4)$ | 3.34(3) | 0.04 |
| Bi-P | 3.82(1) |  | $\mathrm{Pb}(1)-\mathrm{O}(2)-\mathrm{Pb}(4)$ | 114.9(5) | $\mathrm{Pb}(4)-\mathrm{O}(5)$ | 2.98(2) | 0.10 |
| $\mathrm{Bi}-\mathrm{P}$ | 3.85(1) |  | $\mathrm{Pb}(1)-\mathrm{O}(2)-\mathrm{Pb}(4)$ | 107.8(5) | $\mathrm{Pb}(4)-\mathrm{O}(8)$ | 2.70(3) | 0.20 |
|  |  |  | $\mathrm{Pb}(3)-\mathrm{O}(2)-\mathrm{Pb}(4)$ | 102.9(5) |  |  | 2.06 |
| $\mathrm{P}-\mathrm{Pb}(1)$ | 3.89(1) |  | $\mathrm{Pb}(3)-\mathrm{O}(2)-\mathrm{Pb}(4)$ | 104.5(5) |  |  |  |
| $\mathrm{P}-\mathrm{Pb}(1)$ | 3.49(1) |  | $\mathrm{Pb}(4)-\mathrm{O}(2)-\mathrm{Pb}(4)$ | 103.6(5) |  |  |  |
| $\mathrm{P}-\mathrm{Pb}(2)$ | 3.92(1) |  |  |  |  |  |  |
| $\mathrm{P}-\mathrm{Pb}(2)$ | 3.45(1) |  |  |  |  |  |  |
| $\mathrm{P}-\mathrm{Pb}(3)$ | 3.54(1) |  |  |  |  |  |  |
| $\mathrm{P}-\mathrm{Pb}(4)$ | 3.51(1) |  |  |  |  |  |  |

${ }^{a}$ Valence bond sums are indicated in bold.
constitute the equatorial plane of an octahedron with $\mathrm{Pb}(1)$ slightly out of that plane. The apexes are occupied by $\mathrm{O}(2)$ and one $\mathrm{O}(7)$ and they are tilted in the same direction away from the normal to the equatorial plane (Fig. 1b). The triangular face formed by $O(7), O(5), O(8)$ is capped by a second $\mathrm{O}(7)$. The triangular face formed by the apex $\mathrm{O}(7)$ and atoms $\mathrm{O}(3), \mathrm{O}(4)$ is open and the lone pair electrons cap this face. $\mathrm{Pb}(2), \mathrm{Pb}(3)$, and $\mathrm{Pb}(4)$ have similar coordination polyhedra. The articulations of these distorted polyhedra lower the crystal symmetry to triclinic, $\mathrm{P} \overline{1}$, as compared to the monoclinic structure of $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ (14).

It is helpful to visualize this complex structure by describing it in terms of Pb polyhedra around oxygen atoms. Each $\mathrm{O}(1)$ and $\mathrm{O}(2)$ is tetrahedrally surrounded by four Pb (Table 4 and Fig. 2). Two $O(1)$ that are centrosymmetrically related share a tetrahedral edge, $\mathrm{Pb}(3)-\mathrm{Pb}(3)$, and two $\mathrm{O}(2)$ that are similarly related share a tetrahedral edge, $\mathrm{Pb}(4)-\mathrm{Pb}(4)$. In turn the $O(1)$ and $O(2)$ tetrahedra share an edge, $\mathrm{Pb}(3)-\mathrm{Pb}(4)$, to form chains along the $b$-axis (Fig. 2). The phosphate and $\mathrm{Bi}-\mathrm{O}$ groups have tetrahedral and pentagonal pyramidal coordinations, respectively. $\mathrm{O}(6)$ and $\mathrm{O}(7)$ of $\mathrm{PO}_{4}$ connect to Bi to form a chain parallel to the $b$-axis


FIG. 1. (a). The oxygen atom environment around Bi seen along [001]. (b). The oxygen atom environment around Pb . Bond lengths and their standard deviations in $\AA$.


FIG. 2. The Pb environment around oxygen atoms $\mathrm{O}(1)$ and $\mathrm{O}(2)$.
(Fig. 3c). The apical $\mathrm{O}(8)$ of $\mathrm{PO}_{4}$ and $\mathrm{O}(5)$ of the $\mathrm{BiO}_{6}$ units are bonded to four Pb . In turn the Pb atoms also bond by van der Waals contacts to two $\mathrm{O}(7)$ or two $\mathrm{O}(6)$, giving rise to a two-dimensional plane parallel to (100) (Fig. 3). The $\mathrm{Bi}-\mathrm{Pb}, \mathrm{Bi}-\mathrm{P}$, and $\mathrm{Pb}-\mathrm{P}$ bond lengths range from 3.45 to $3.92 \AA$, similar to those in related compounds $(7,14)$.

The $\mathrm{Pb}-\mathrm{O}$ frameworks in tetragonal PbO (20), in $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ (14), and in $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$, (Figs. 3a-3c) display corrugated $\mathrm{Pb}-\mathrm{O}$ chains. In PbO the chains are parallel to the $b$-axis and are linked so that the Pb atoms of two chains form a trigonal prism (Fig. 3a). In $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ the chains are parallel to the $a$-axis and link to form a trigonal prism moiety that is distorted because the large $\mathrm{SO}_{4}$ group alternates with Pb in the sixth position (Fig. 3b). In $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ the sixth position is occupied by either Bi or $\mathrm{PO}_{4}$ (Fig. 3c). In PbO the layers are linked by weak $\mathrm{Pb}-\mathrm{Pb}$ van der Waals contacts. In $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ (Fig. 4a), the parallel chains are linked by strong $\mathrm{O}-\mathrm{Pb}-\mathrm{O}$ bonds. Finally in $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ (Fig. 4b), the basic units are linked by strong $\mathrm{O}(3)-\mathrm{Bi}-\mathrm{O}(5)$ bonds and weak $\mathrm{O}(6)-\mathrm{Bi}(3.15 \AA)$ and $\mathrm{O}(7)-\mathrm{Bi}(3.10 \AA)$ bonds. This $\mathrm{Pb}-\mathrm{O}$ structural motif lends itself readily to the replacement of the $\mathrm{PO}_{4}$ moiety by other tetrahedral groups such as $\mathrm{SO}_{4}$ and $\mathrm{AsO}_{4}$ and Bi by other trivalent ions of similar ionic radius. We , however, could not synthesize a hypothetical isostructural phase, $\mathrm{Pb}_{4} \mathrm{LaPO}_{8}$.

Within experimental error the phosphorus atoms are in a nearly regular tetrahedral oxygen environment (Table 5),


FIG. 3. The crystal structure motifs of (a) tetragonal PbO , (b) $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ projected on (100), and (c) $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$ projected on (011).


FIG. 3-Continued


FIG. 4. Linkages between the structural motifs in (a) $\mathrm{Pb}_{5} \mathrm{SO}_{8}$ and (b) $\mathrm{Pb}_{4} \mathrm{BiPO}_{8}$.


FIG. 4 -Continued
with four $\mathrm{P}-\mathrm{O}$ bond lengths contributing to a valence bond sum (21) of 5.14, close to the $\mathrm{P}^{5+}$ expected oxidation state. The $\mathrm{Pb}(1)$ oxygen coordination polyhedron has been previously described. The inclusion of these seven $\mathrm{Pb}-\mathrm{O}$ bonds in the valence bond sum calculation yields 2.63 , well over the $2^{+}$oxidation state. The valence bond sum calculated for $\mathrm{Pb}(2)$ is 2.32 , while more normal values, 2.14 and 2.06 , are calculated for $\mathrm{Pb}(3)$ and $\mathrm{Pb}(4)$. The valence bond sum for Bi is 2.14 , much less than the expected trivalent oxidation state. Thus the high valence bond sums of $\mathrm{Pb}(1)$ and $\mathrm{Pb}(2)$ appear to compensate for the decrease of the Bi oxidation state. Interchanging $\mathrm{Pb}(1)$ and Bi leaves the structural parameters unchanged because of the nearly identical scattering power of the atoms. Further, such an interchange disrupts the Pb framework. We are certain that the atom assignment is correct. A low valence bond sum for Bi was observed in $\mathrm{Pb}_{2} \mathrm{BiPO}_{6}$ but there was compensated by an unusual 6.07 valence bond sum for P (7). Using the van der Waals radii for Pb and Bi as 2.02 and $1.82 \AA$, respectively, the contacts between $\mathrm{Pb}(1), \mathrm{Pb}(2)$, and Bi are $3.73 \AA$ but no contacts exist between $\mathrm{Pb}(3), \mathrm{Pb}(4)$, and Bi . It is postulated that where van der Waals contacts for $\mathrm{Pb}-\mathrm{Bi}$ exist the $\mathrm{Pb} 6 \mathrm{~s}^{2}$ energy levels
overlap the empty Bi 6 p energy levels so that electron transfer into the Bi 6 p levels from Pb occurs. The electrons are not itinerant because of the large atomic separations and the material remains insulating.

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## REFERENCES

1. V. V. Volkov, L. A. Zhereb, Y. F. Kargin, V. M. Skorikov, and I. V. Tananeav, Russ J. Inorg. Chem. 28, 1002 (1983).
2. J. P. Wignacourt, M. Drache, P. Conflant, and J. C. Boivin, J. Chim. Phys. 88, 1933 (1991).
3. Y. A. Blinovskov and A. A. Fotiev, Russ. J. Inorg. Chem. 32, 145 (1987).
4. Akiteru Watanabe, Solid State Ion. 96, 75 (1997).
5. A. Mizrahi, J. P. Wignacourt, M. Drache, and P. Conflant, J. Mater. Chem. 5(6), 901 (1995).
6. Y. C. Jie and W. Eysel, Powder Diffr. 9, 1 (1994).
7. A. Mizrahi, J. P. Wignacourt, and H. Steinfink, J. Solid State Chem. 133, 516 (1997).
8. K. Sahl, Z. Kristallogr. 141, 145 (1975).
9. B. F. Mentzen, J. C. Viala, A. Sartre, and J. Bouix, C. R. Acad. Sci. Paris 293, Série II, 1053 (1981).
10. T. Negas, J. Am. Ceram. Soc. 51, 716 (1968).
11. H. Bode and E. Voss, Electrochim. Acta 1, 318 (1959).
12. Y. Watanabe and Y. Otsubo, Nipp, Kagakukaishi 8, 1603 (1973).
13. D. B. Nihtianova and V. I. Ivanov, Z. Kristallogr. 212, 191 (1997).
14. Ian M. Steele and Joseph J. Pluth, J. Electrochem. Soc. 145, 528 (1998).
15. P. E. Werner, L. Eriksson, and M. Westdahl, J. Appl. Crystallogr. 18, 367 (1985).
16. G. M. Sheldrick, "SHELXTL Plus Crystallographic System." Siemens Analytical X-Ray Instruments, Madison, WI, 1989.
17. Sheldrick, "SHELXS86." Institut Anorganische Chemie, Göttingen, 1985.
18. G. M. Sheldrick, "SHELXL-93." Institut Anorganische Chemie, Göttingen, 1993.
19. Ron Jenkins and Robert L. Snyder, "Introduction to X-Ray Powder Diffractometry." Wiley, New York, 1996.
20. R. G. Wyckoff, "Crystal Structures," Wiley-Interscience, New York, 1963.
21. D. Brown and D. Altermatt, Acta Crystallogr. B 41, 244 (1985).

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